# SRI RAMAKRISHNA MISSION VIDYALAYA COLLEGE OF ARTS AND SCIENCE

(Autonomous) COIMBATORE – 641 020



# DEPARTMENT OF MATHEMATICS

# Under Choice Based Credit System (CBCS) 2017 – 2018 Onwards

**M.Sc. MATHEMATICS** 

SEM	IESTER – I							
S.	Course code	Title of the paper	Hrs	Cre	Exam	Maximum Marks		
No				dits	Hour s	Int	Ext	Total
01	17PMA1C01	Algebra	6	5	3	25	75	100
02	13PMA1C02	Real Analysis	6	5	3	25	75	100
03	17PMA1C03	Ordinary Differential Equations	6	5	3	25	75	100
04	17PMA1C04	Mathematical Statistics	4	3	3	25	75	100
05	13PMA1EL1	Elective 1: Numerical Analysis	5	4	3	25	75	100
06	13PMA2CP1	Core Practical: Mathematical software – I and II	3	-	_	-	-	-
	TOTAL – I		30	22				500

## **M.SC., MATHEMATICS** SCHEME OF EXAMINATIONS

SEN	IESTER II							
S.	Course code	Title of the paper	Hrs	Cre	Exam	Max	imum 🛛	Marks
No				dits	Hour s	Int	Ext	Total
01	13PMA2C05	Complex Analysis	6	5	3	25	75	100
02	13PMA2C06	Partial Differential Equations	6	4	3	25	75	100
03	17PMA2C07	Mechanics	6	4	3	25	75	100
04	13PMA2C08	Mathematical Software II : (Programming in C++)	4	3	3	25	75	100
05	13PMA2EL2	Elective 2: Graph Theory	5	4	3	25	75	100
06	13PMA2CP1	Core Practical: Mathematical software – I and II	3	3	3	40	60	100
	ТО	TAL – II	30	23				600

SEN	SEMESTER III								
S.	Course code Title of the paper		Hrs	Cre	Exam	Maximum marks			
No				dits	Hour	Int	Ext	Total	
					S				
01	13PMA3C09	Topology	6	5	3	25	75	100	
02	13PMA3C10	Nonlinear Differential Equations	6	4	3	25	75	100	
03	16PMA3C11	Combinatorics	6	4	3	25	75	100	
04	17PMA3C12	Mathematical software -III MATLAB	5	4	3	25	75	100	
05	13PMA3EL3	Elective 3(IDE): Relativity and Wave Mechanics	5	4	3	25	75	100	
06	13PMA4CP2	Core Practical: Mathematical Software - III	2	-	-	-	-	-	
	TOTAL – III		30	21				400	

SEMESTER IV									
S.	Course code	Title of the paper	Hrs	Cre	Exam	Max	<b>imum</b> I	num Marks	
No				dits	Hour s	Int	Ext	Total	
01	13PMA4C13	Functional Analysis	6	5	3	25	75	100	
02	17PMA4C14	Mathematical Methods	6	4	3	25	75	100	
03	13PMA4C15	Differential Geometry	5	4	3	25	75	100	
04	13PMA4EL4	Elective 4: Fluid Dynamics	6	4	3	25	75	100	
05	13PMA4EL5	Elective 5: Control Theory	5	4	3	25	75	100	
06	13PMA4CP2	Core Practical: Mathematical Software - III	2	3	3	40	60	100	
	TOTAL – IV		30	24				700	

## SRI RAMAKRISHNA MISSION VIDYALAYA COLLEGE OF ARTS AND SCIENCE (AUTONOMOUS) COIMBATORE – 641 020. For candidates admitted from academic year 2017-2018 onwards Under New CBCS

: M.Sc. Mathematics

<b>Course Title</b>	: CORE 1: ALGEBRA	Subject Code	e: 17PMA1C01
Year	: First Year	Semester	: I
Hours/Week	: 6	Credits	: 5

#### Unit I:

Programme

**Group Theory:** Another counting principle - Sylows Theorem. Chapter 2: Sections 2.11 and 2.12

### Unit II:

**Ring Theory:**Euclidean Rings- Particular Euclidean Ring - Polynomial Rings - Polynomials over the Rational Field. **Chapter 3: Sections 3.7 to 3.10** 

#### Unit III:

**Fields:**Extension field – Roots of polynomials. **Chapter 5: Sections 5.1 and 5.3** 

#### Unit IV:

**Fields:** More about roots - Elements of Galois Theory. **Chapter 5: Sections 5.5 and 5.6** 

### Unit V:

**Linear Transformations**: Canonical Forms: Triangular form, Trace and Transpose – Hermitian, Unitary and Normal Transformations. **Chapter 6: Sections 6.4, 6.8 and 6.10** 

#### Treatment as in:

Topics in Algebra by I.N. Herstein, John Wiley & Sons, Second Edition, 2006.

#### **References:**

1. Algebra by M. Martin, Prentice Hall of India, New Delhi, 1991.

2. A First Course in Abstract Algebra by J. B. Fraleigh, V Ed., Addison-

Wesley Longman, Inc., Reading Massachusetts, 1999.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

**Programme** : M.Sc. Mathematics.

Course Title: CORE 2: REAL ANALYSISYear: First YearHours/Week: 6Riemann Stieltjes Integral

Subject Code : 13PMA1C02 Semester : I Credits : 5

## Unit I:

**Riemann Stieltjes Integral:** Definition and existence of the integral – Properties of the integral – Integration and Differentiation – Integration of vector valued function – Rectifiable curves.

Chapter : 6

## Unit II:

Uniform convergence and continuity - Uniform convergence and integration -Uniform convergence and differentiation – equicontinuous families of functions – The Stone – Weirstrass theorem.

## Chapter:7

## Function of Several Variables:

## Unit III:

Linear Transformation – The Contraction principle – The Inverse Function Theorem – Implicit Function Theorem – Determinants – Derivatives of Higher order – Differentiation of integrals.

## Chapter: 9

## Lebesgue Measure:

## Unit IV:

**Lebesque Measure**: Outer measure – Measurable sets and Lebesque measure – Measurable functions.

## Chapter 3: Sections 3.2 - 3.4

## Unit V:

**Lebesque Integral:** The Lebesque integral of a bounded functions over a set of finite measure – integrals of a non-negative functions – General Lebesque integral.

Chapter 4: Sections: 4.2 - 4.4

## Treatment as in:

1. Principles of Mathematical Analysis, Walter Rudin, Third Edition,

1976. (Units I, II and III)

2. Real Analysis by H.L. Royden, 3<sup>nd</sup> edition, Macmillan, New york, 1988. (Units IV and V).

### For candidates admitted from academic year 2017-2018 onwards Under New CBCS

Programme : M.Sc. Mathematics. Course Title : CORE 3: ORDINARY DIFFERENTIAL EQUATIONS Subject Code:17PMA1C03 Year : First Year Semester : I Hours/Week : 6 Credits : 4

#### Unit I:

**System of Linear Differential Equations:** Introduction - System of first order equations – Existence and Uniqueness theorem – Fundamental Matrix. **Chapter 4: Section 4.1 - 4.5** 

#### Unit II:

**System of Linear Differential Equations:** Non – Homogeneous linear systems: Linear systems with constant co-efficient - Linear systems with periodic co-efficient.

### Chapter 4: Section 4.6 - 4.7

#### Unit III:

**Existence and Uniqueness of Solutions**: Introduction - Preliminaries-Successive Approximation - Picard's theorem - Non-uniqueness of solutions- Continuation and dependence on initial conditions - Existence of solutions in the large - Existence and Uniqueness of solution of systems.

## Chapter 5: Section 5.1 - 5.8

#### Unit IV:

**Boundary Value Problems**: Introduction - Sturm Liouville problem – Green's Functions – Non Existence of Solutions.

## Chapter 7: Section 7.1 - 7.4

#### Unit V:

**Oscillations of Second Order Equations:** Fundamental results - Sturm's Comparision theorem - Elementary linear Oscillations - Comparision theorem of Hille – Wintner Oscillations of X'' + a(t) X=0, Elementary nonlinear oscillations. **Chapter 8: Section 8.1 - 8.6** 

#### Treatment as in:

Text book of Ordinary Differential Equations by S.G. Deo,

**V. Lakshmikanthan and V. Ragavendra**, Tata McGraw-Hill Publishing Company Limited, 2010.

#### **Reference Book:**

**Ordinary Differential Equations A First Course by D. Somasundaram,** Narosa Publishing House, Fourth Edition, New Delhi, 2010.

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Programme · M Sc Mathematics

1 rogramme	· Misc. Mau	icinatics.					
Course Title : CORE 4: MATHEMATICAL			CAL	Subject Code : 17PMA1C04			
STATISTIC	S						
Year	: First Year			Sem	lester	: I	
Hours/Week	: : 5			Cre	dits	:4	
Unit I:							
_			<b>a b</b>				

**Parameters of the Distribution of a Random Variable**: Expected values – Moments – The Chebyshev inequality – Absolute moments- order of parameters-Moments of random vectors. **Chapter 3: Sections 3.1 - 3.6** 

Unit II:

**Characteristic Functions**: Properties of Characteristic functions and moments – Semi invariants – The Characteristic function of the sum of independent random variables – Determination of distribution functions by the characteristic functions-Probability generating functions.

Chapter: 4: Sections 4.1 -4.5, 4.7.

#### Unit III:

**Some Probability Distribution:** One point and two point Distributions – The Binomial distribution – The Poisson distribution – Normal Distribution – Uniform Distribution – Gamma Distribution – Beta Distribution. **Chapter: 5 Sections 5.1, 5.2, 5.5 - 5.9.** 

#### Unit IV:

Limit Theorems: Stochastic Convergence – Bernoulli's Law of large numbers – Levy Cramer theorem – De Moivre- Laplace theorem – The Lindeberg-Levy theorem. Chapter: 6 Sections 6.2, 6.3, 6.6, 6.7, 6.8.

#### Unit V:

**The Notion of a Sample:** The notion of a statistic – The distribution of the arithmetic mean of independent normally distributed random variables – The Chi- square distribution- Distribution of the statistic ( $\overline{X}, S$ )- Student's t-distributions.

Chapter: 9 Sections 9.1 - 9.6

#### Treatment as in:

1. **Probability Theory and Mathematical Statistics, Marek Fisz,** John Wiley, Third Edition, New York, 1963.

#### **Reference Book:**

1. An Introduction to Probability Theory and its Applications, W. Feller, Vol. I, John Wiley, Third Edition, 1968.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.	
<b>Course Title</b>	: Elective 1: NUMERICAL ANALYSIS	Subject Code : 13PMA1EL1
Year	: First Year	Semester : I
Hours/Week	:5	Credits : 4

### Unit I:

**Solution of Non-Linear Equations:** Method of halving the interval – Method of linear interpolation – Newton's method – Use of X = G(X) form - convergence of Newton's method – Bairstow's method for Quadratic factors – Quotient-difference algorithm.

Chapter 1: Sections 1.2 -1.4, 1.6 – 1.9

### Unit II:

**Solution of System of Equations**: Elimination method – Gauss and Gauss Jordan methods – LU Decomposition method - Methods of iteration – Relaxation method – Set of Non-linear equations.

Chapter 2: Sections 2.3, 2.4, 2.5, 2.10, 2.11, 2.12

## Unit III:

Solution of Ordinary Differential Equations: Taylor series method – Euler and Euler Modified methods – Runge-Kutta Methods – Multistep Methods – Milne's method – Adams Moulton method.

Chapter 5: Sections 6.2 – 6.7

### Unit IV:

## **Boundary Value Problems and Characteristic Value Problems:**

The shooting method – solution through a set of equations – Derivative of Boundary conditions – Characteristic value problems – Eigen values of a matrix by Iteration.

## Chapter 6: Sections 7.2 – 7.5

Unit V:

## **Types of Partial Differential Equations:**

The Heat equation and the Wave equation- Solution Techniques for the Heat equation in One Dimensional – Solving the Vibrating String Problem – Parabolic Equations in Two or Three Dimensions – The Wave Equation in Two Dimensions.

Chapter 8: Sections 8.1 – 8.6

**Treatment as in: Applied Numerical Analysis by C.F. Gerald and P.O.Wheatley**, Pearson Education, 6<sup>th</sup> Edition, 2003.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.		
<b>Course Title</b>	: CORE 5: COMPLEX ANALYSIS	Subject Code	: 13PMA2C05
Year	: First Year	Semester	: II
Hours/Week	: 6	Credits	: 5

#### Unit I:

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**Complex Integration:** Cauchy's integral formula – local properties of analytic functions – the calculus of residues.

Chapter 4: Sections 2.1 - 2.3, 3.1, 3.2, 3.4, 5.1 - 5.2

## Unit II:

**Harmonic Functions**: Series and product development: power series expansions.

Chapter 4: Sections 6.1- 6.3; Chapter V: Sections 1.1 - 1.3

### Unit III:

Partial Fractions and Factorizations – Entire functions. Chapter 5: Sections 2.1, 2.4, 3.1 - 3.2.

### Unit IV:

**Conformal Mapping, Dirichlet Problem**: Conformal mapping of polygons, A closer look at harmonic functions, The Dirichlet problem **Chapter 6: Sections 2.1, 2.2, 3.1, 3.2, 4.1 and 4.2.** 

#### Unit V:

**Elliptic Functions**: Simply periodic functions, Doubly periodic functions. Chapter 7: Sections 1.1 - 1.3, 2.1 - 2.4.

### **Treatment as in:**

**Complex Analysis by Lars. V. Ahlfors**, McGraw Hill, International Edition (Third Edition) 1979.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme: M.Sc. Mathematics.Subject Code: 13PMA2C06Course Title: CORE 6 : PARTIAL DIFFERENTIAL EQUATIONSYear: First YearSemester : IIHours/Week: 6Credits: 5

#### Unit I:

Partial Differential Equations- nonlinear PDE of first order compatible system of first order equations- Charpit's method-special type of first order equation- Jacobi method. Chapter 2: Sections 1, 7, 9, 10, 11 and 13.

#### Unit II:

**Partial Differential Equations of the second order** : Linear partial differential equation with constant coefficients - Equations with variable co efficients **Chapter 3: Sections 4 and 5.** 

#### Unit III:

**Laplace's Equation:** Occurrence of Laplace equation in physics –Elementary solution of Laplace equation – Boundary value problem separation of variables-Problems with axial symmetry –Kelvin's theorem –Theory of Green's functions-Relations of Dirichlet problem to calculus of variables –Two dimensional Laplace Equation –Green function for two dimensional equation. **Chapter 4: Sections 1, 2, 4, 5, 6, 7, 8, 9, 11 and 13.** 

#### Unit IV:

**The Wave Equation:** Occurrence of wave function in Physics –Elementary solution one dimensional wave equation vibrating membranes-Application of calculus of variation-Three dimensional problem-General solution of wave equation-Green's function for wave equation-Non homogeneous wave equation. **Chapter 5: Sections 1, 2, 4, 5, 6, 7 and 8.** 

#### Unit V:

**The Diffusion Equation**: Occurrence of Diffusion equation in Physics –Resolution of boundary value problem for diffusion equation-Elementary solution of diffusion equation –Separation of variables-Use of Green's functions. **Chapter 6: Sections 1, 2, 3, 4 and 6.** 

### Treatment as in:

Elements of Partial Differential Equations by I.N. Sneddon, McGraw Hill, 1988.

#### For candidates admitted from academic year 2017-2018 onwards **Under New CBCS**

0	: M.Sc. Mathematics.		
<b>Course Title</b>	: CORE 7: MECHANICS	Subject Code	:17PMA2C07
Year	: First Year	Semester	: II
Hours/Week	:6	Credits	:4

#### Unit I:

Introductory Concepts: The Mechanical System - Geometrical co-ordinates -Constraints Virtual Work - Energy. Chapter 1: Sections 1.1 – 1.5

#### Unit II:

**Lagrange's Equations:** Derivation of Lagrange's Equations – Integral of the motion-

Natural system and Liouvilles systems & Examples Chapter 2: Sections 2.1 - 2.3

#### Unit III:

## Hamilton's Equations:

Hamilton's Principle – Hamilton's Equations – Modified Hamilton's Principle – Principle of least action and examples Chapter 4: Sections 4.1 - 4.3

#### Unit IV:

Hamilton-Jacobi Theory: Hamilton's Principle function – The Hamilton – Jacobi Equation. Chapter 5: Sections 5.1 - 5.2.

#### Unit V:

#### **Canonical Transformations:**

Differential forms and generating functions – Lagrange and Poisson brackets. Chapter 6: Sections 6.1 - 6.3

#### Treatment as in:

Classical Dynamics by D. T. Greenwood, Prentice Hall (1985).

Reference Book: Classical Mechanics by Herbert Golstein, Charles poole, John safko, Addson Wesley, Third edition, 2000.

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**Programme** : M.Sc. Mathematics.

Subject Code:13PMA2C08

**Course Title : Core 8 - Mathematical Software II : (Programming in C++)** 

Year : First Year Hours/Week : 4 Semester : II Credits : 3

### Unit I:

**Principle of Object Oriented Programming:** Object oriented programming paradigm. Basic concepts of object oriented programming structure of C++ program. Tokens – keywords – identities – Basic Data types – User-Defined Data types – Derived Data types – symbolic constants – Type compatibility – Declaration of variables – Dynamic Initialization of variables – reference variables. **Section: 1.4 & 1.5, 3.2 – 3.12** 

#### Unit II:

Operators in C++ - Scope Resolution operator – Member Dereferencing operators – Memory Management operators – Type cast operator – Expressions and Implicit conversions – Operator overloading – Operator Precedence. Functions in C++ -Introduction – The main function – Function Prototyping –Call by Reference – Return by Reference – Inline functions – Default Arguments – Constant Arguments.

### Section: 3.13 – 3.16, 3.18 – 3.21, 4.1 – 4.8

#### Unit III:

**Classes and Objects:** Introduction – Specifying a class – Defining Members Functions – Making an outside function inline – Nesting of Member Functions – Private Member Functions – Arrays within a class – Memory Allocation for Objects – Static Data Members – Static Member Functions – Friendly functions – Returning objects – Const Member Functions. **Constructors and Destructors:** Introduction – Parameterized Constructors - Multiple Constructors in a class – Constructors with Default Arguments.

Section: 5.1, 5.3, 5.4, 5.6 – 5.12, 5.16 – 5.17, 6.1- 6.5.

#### Unit IV:

**Operator Overloading and Type Conversions:** Introduction – Defining operators overloading – Overloading Unary operators – Overloading Binary operators using friends – Manipulation of strings using operators. Rules for overloading operators – Type conversion. **Inheritance: Extending Classes:** Introduction – Defining Derived classes – Single Inheritance – Making a private Member inheritable – Multilevel Inheritance – Multiple Inheritance – Hierarchical Inheritance – Hybrid Inheritance.

### Sections: 7.1 -7.8, 8.1 – 8.8.

### Unit V:

Pointers, Virtual Functions and Polymorphism:Introduction – Pointers to objects- 'This' pointer – pointer to Derived classes –Virtual Functions – Pure VirtualFunctions. Managing Console I / O Operations:Introduction – C++ Streams – C++stream classes – Unformatted I / O operations – Formatted console I / O operations –Managing output with Manipulators.

## Sections: 9.1 – 9.6, 10.1 – 10.6.

#### Treatment as in:

Object – Oriented Programming with C ++ by E. Balagurusamy, Tata McGraw – Hill, New Delhi, 1998.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.
<b>Course Title</b>	: Elective 2: GRAPH THEORY
Year	: First Year
Hours/Week	: 5

<b>Subject Code</b>	: 13PMA2EL2
Semester	: II
Credits	:4

## Unit I:

Introduction - Paths and Circuits

Chapter1: Sections 1.1 -1.5 Chapter 2: Sections 2.1- 2.2, 2.4-2.10

## Unit II:

Trees and fundamental circuits - Cut sets and cut vertices Chapter3: Sections 3.1 -3.4, 3.7-3.10 Chapter 4: Sections4.1 -4.5

## Unit III:

Planar and Dual graphs -Vector spaces of a graph -Chapter 5: Sections 5.1 -5.4, 5.6-5.9 Chapter 6: Sections 6.1 – 6.9

## Unit IV:

Matrix representation of graph -Coloring, Covering and Partitioning Chapter 7: Sections 7.1 – 7.9 Chapter 8: Sections 8.1- 8.6

## Unit V:

Direct graph Chapter 9: Sections 9.1- 9.5, 9.8-9.11

### **Treatment as in:**

**Graph Theory with Applications to Engineering and Computer Science by Narsingh Deo**, Prentice Hall, 2007.

<b>Course Title</b>	: Core Practical:	Mathematical software	e – I and II	
Course Code : 1	I3PMA2CP1			
Year	: First Year		Semester	: II
Hours/Week/	: 3 for two Semest	ers	Credits	: 2

## LIST OF EXPERIMENTS

## **SPSS PRACTICALS:**

1. Mean, Median, Mode, Standard Deviation for individual data and discrete

data.

- 2. Skewness and Kurtosis for individual data and discrete data.
- 3. Test of significance based on t- test (independent sample t-test).
- 4. Chi- square test for goodness of fit.
- 5. ANOVA table.

## C + + PRACTICAL:

- 1. Expressing a given number as a product of primes
- 2. To convert the given 2 set of times calculated as day, hour, minutes and seconds.
- 3. Binary search.
- 4. Various types of Correlation.
- 5. Regression Analyss.
- 6. Standard and Mean Deviation.
- 7. Bisection Method.
- 8. Newton Raphson Method.
- 9. R-K method of fourth order.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.		
<b>Course Title</b>	: CORE 9: TOPOLOGY	Subject Code	e : 13PMA3C09
Year	: Second Year	Semester	: III
Hours/Week	: 6	Credits	: 5

#### Unit I:

**Topological Spaces and Continuous Functions:** Topological spaces – Basis for a Topology – The Order topology – The Product topology on X x Y – The Subspace topology – Closed sets and limit points. **Chapter 2: Sections 12 - 17** 

#### Unit II:

**Topological Spaces and Continuous Functions:** Continuous functions – The Product topology – The Metric topology. **Chapter 2: Sections 18 - 20** 

#### Unit III:

**Connectedness and Compactness:** Connected spaces – Connected Subspaces of the real line – Components and Local Connectedness. **Chapter 3: Sections 23 - 25** 

#### Unit IV:

**Connectedness and Compactness:** Compact spaces, Compact Subspaces of the real line – Limit point compactness. **Chapter 3: Sections 26 - 28** 

#### Unit V:

**Countability and Separation Axioms:** The Countability Axioms – The Separation Axioms – The Urysohn Lemma – The UrysohnMetrization theorem. **Chapter 4: Sections 30, 31, 33, 34** 

#### Treatment as in:

Topology by James R. Munkres, Prentice Hall of India, New Delhi, 2007.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.	Subject Code	e :13PMA3C10
<b>Course Title</b>	: CORE 10: Nonlinear Differential Equat	tions	
Year	: Second Year	Semester	: IV
Hours/Week	:6	Credits	: 5

## Unit I:

**First order systems in two variables and linearization**: The general phase plane – some population models – linear approximation at equilibrium points – The general solution of a linear system. **Chapter 2: Sections 2.1 - 2.4** 

#### Unit II:

**Averaging Methods**: An energy balance method for limit cycles – Amplitude and frequency estimates – Slowly varying amplitudes: Nearly periodic solutions – Periodic solutions: Harmonic balance – Equivalent linear equation by harmonic.

## Chapter 4: Sections 4.1 - 4.5

### Unit III:

**Perturbation Methods:** Outline of the direct method – Forced Oscillations far from resonance – Forced oscillations near resonance with weak excitation – Amplitude equation for undamped pendulum– Lindstedt's method – The perturbation method and Fourier series.

Chapter 5: Sections 5.1 - 5.4, 5.8, 5.10.

## Unit IV:

**Stability:** Poincare stability – Solutions, paths and norms – Liapunov stability. Stability of linear systems- Stability and boundedness for linear systems-Stability of system with constant coefficients.

Chapter 8: Sections 8.1 – 8.4, 8.6-8.7.

### Unit V:

**The Existence of Periodic solutions:** The Poincare-Bendixson theorem-Atheorem on the existence of a centre-A theorem on the existence of a limit cycle- Van der Pol's equation with large parameter.

## **Chapter 11: Sections 11.1 – 11.4**

## Treatment as in:

Nonlinear Ordinary Differential Equations by D.W. Jordan and P. Smith, Clarendon Press, Oxford, Second Edition, 1987.

## **References:**

- 1. **Differential Equations by G.F. Simmons**, Tata McGraw-Hill, New Delhi, 1979.
- 2. Ordinary Differential Equations and Stability Theory by D.A. Sanchez, Dover, New York, 1968.

For candidates admitted from academic year 2016-2017 onwards Under New CBCS

Programme: M.Sc. Mathematics.Course Title: CORE 11: COMBINATORICSYear: Second YearHours/Week: 6

Subject Code : 16PMA3C11 Semester : I Credits : 4

#### Unit I:

Selection and Binomial coefficients: Permutations - Ordered selections - Unordered selections - Further remarks on the Binomial theorem - Miscellaneous problems. Chapter:2 Sections 2.1-2.5.

#### Unit II:

**Paring problems**: Pairing within a set - Pairing between sets - An optimal assignment problem - Gale's optimal assignment problem - Further reading . **Chapter: 3 Sections 3.1 - 3.5.** 

### Unit III:

**Recurrence** :Some miscellaneous problems-Fibonacci - type relations - using generating functions - Miscellaneous methods - Counting simple electrical networks. **Chapter: 4 Sections 4.1-4.5.** 

#### Unit IV:

**The Inclusion – Exclusion principle:** The principle - Rook polynomials. **Steiner systems and sphere packing's :** Introductory remarks – Steiner system - S(5,8,24). **Chapter: 5 Sections 5.1, 5.2** 

**Chapter: 7 Sections 7.1 – 7.3** 

### Unit V:

Block design and Error –Correcting codes: Block designs- Square block design-Hadamard configurations- Error- Correcting codes. Chapter: 6 Sections 6.1 - 6.4

### Treatment as in:

#### A First Course in Combinatorial Mathematics by IAN ANDERSON, Clorendon press, Oxford 1974

Clorendon press, Oxford, 1974.

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Programme	: M.Sc. Mathematics.	Subject Code	e :17PMA3C12
<b>Course Title</b>	: CORE 12: Mathematical Software – II	II MATLAB	
Year	: Second Year	Semester	: III
Hours/Week	:5	Credits	: 4

#### Unit I:

**Introduction:** What is MATLAB? - Does MATLAB do symbolic calculations? -Will MATLAB run on my computer? - Where do I get MATLAB? - How do I use this book?-Basic of MATLAB, Input – Output - File types – Platform dependence – General commands.

Chapter I: Section 1.1-1.6

#### Unit II:

**Interactive Computation:** Matrices and vectors – Matrix and Array Operations – Creating and Using Inline functions – Using Built-in Functions and On-line Help – Saving and loading data – Plotting simple graphs. **Chapter III: Sections 3.1 – 3.6.** 

#### Unit III:

**Programming in MATLAB:** Scripts and Functions – Script files – Function files – Language specific features – Advanced data objects. **Chapter IV: Sections 4.1 – 4.4.** 

#### Unit IV:

**Applications:**Linear Algebra – Curve fitting and Interpolation – Data analysis and Statistics – Numerical Integration – Ordinary differential equations – Nonlinear Algebraic Equations.

Chapter V: Sections 5.1 – 5.6.

### Unit V:

**Graphics**: Basic 2-D plots – Using subplot to layout multiple graphs – 3-D Plots – Handle Graphics – Saving and Printing Graphs – Errors. **Chapter VI & VII: Sections 6.1 – 6.5.** 

#### **Treatment as in:**

Getting started with MATLAB – A Quick Introduction for Scientists and Engineers by Rudra Pratap, Oxford University Press, 2003.

Course Title: PRACTICAL: Mathematical Software - 3 MATLABCourse Code: 13PMA4CP2Year: Second YearHours/Week: 3 for Two SemestersCredits: 2

## Mat Lab Practical:

## 1. Equation of Straight line

2. Multiply, divide and exponentiate vectors

- 3. Points on a circle
- 4. Geometric series
- 5. Matrices and vectors
- 6. Simple sine plot
- 7. Exponentially decaying sine plot
- 8. Log scale plots
- 9. Overlay plots
- 10. Temperature conversion
- 11. Factorial calculation
- 12. Solution of a system of linear equations
- 13. Eigen value and Eigen vectors
- 14. Curve fitting and interpolation
- 15. Mean, Median and Standard Deviation
- 16. Numerical Integration
- 17. Double integration
- 18. Ordinary Differential Equation
- 19. RungeKutta method
- 20. Newton Rapson method

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.		
<b>Course Title</b>	: CORE 13: FUNCTIONAL ANALYSIS	Subject Code	: 13PMA4C13
Year	: Second Year	Semester	: IV
Hours/Week	:6	Credits	: 5

#### Unit I:

**Banach Spaces:** The definition and some examples – Continuous Linear Transformation – The Hahn – Banach theorem. **Chapter 9: Sections 46 – 48** 

### Unit II:

The natural imbedding of N in N\*\* - The Open Mapping Theorem – The conjugate of an operator. **Hilbert spaces**: The Definition and some examples - properties. **Chapter 9: Sections 49 -51** and **Chapter 10: Section 52** 

### Unit III:

Orthogonal complements – Orthogonal sets – The conjugate space H\* - The Adjoint of an Operator.

Chapter 10: Sections 53 – 56

#### Unit IV:

Self – Adjoint operators – Normal and Unitary operators – Projections Chapter 10: Sections 57 -59

#### Unit V:

**Finite – dimensional Spectral Theory:** Matrices – The Spectral theorem **General Preliminaries on Banach Algebras:** The Definition and some examples – Regular and singular elements. **Chapter 11: Sections 60 – 62** and **Chapter 11: Sections 64, 65** 

#### Treatment as in:

**Introduction to Topology and Modern Analysis by G. F. Simmons**, McGraw Hill publication Company, 1963.

#### SRI RAMAKRISHNA MISSION VIDYALAYA COLLEGE OF ARTS AND SCIENCE (AUTONOMOUS) COIMBATORE - 641 020. For candidates admitted from academic year 2017-2018 onwards **Under New CBCS**

**Programme** : M.Sc. Mathematics.

Course Title : CORE 14: MATHEMATICAL METHODS Subject Code :17PMA4C14 Year : Second Year Semester : IV

Hours/Week : 6

Credits

:4

Unit I:

Fourier Transforms, Finite Fourier Transforms, Applications of Fourier Transforms in Initial and Boundary value problems.

Chapter 6: Sections 6.1, 6.4 -6.12, Examples 1 – 5, 13 - 19

Chapter 7: Sections 7.1 - 7.4, Examples 1 - 9

Chapter 8: (Omit miscellaneous exercises.)

## Unit II:

Henkel Transforms and finite Hankel Transforms, Applications of Hankel Transforms in Initial and Boundary value problems.

Chapters: 9, 10, 11

## Unit III:

Introduction: Definition - Regularity Conditions - Special kinds of Kernels -Eigenvalues and Eigenfunctions – Convolution Integral – The inner or scaler product of two functions. Integral Equations with Separable Kernels: Reduction to a system of Algebraic equations – Examples – Fredholm Alternative – Examples – An Approximate Method. Method of Successive Approximations: Iterative Scheme -Examples – Volterra Integral Equation – Examples.

Chapter I: Sections 1.1 – 1.6, Chapter II: Sections 2.1 – 2.5 and Chapters III: Sections 3.1 – 3.4

## Unit IV:

Application Integral Equation to Ordinary Differential EquationInitial value problems, Boundary value problems – Examples Singular Integral Equation Abel integral equation - Examples.

Chapter 5: Sections 5.1 – 5.3 and Chapter 8: Sections 8.1 – 8.2

## Unit V:

**Calculus of Variations**: Variation and its properties – Euler's equation – functionals of the form functional dependent on higher order derivatives- functional dependent on the functions of several independent variables variational problem in parametric form.

## **Chapter 6: Sections 6.1 - 6.7.**

## Treatment as in:

- Integral transforms by Vasistha and Gupta, Krishna PrakasamMandir 1. Meerut, 1993-94. For Units I & II.
- Linear Integral Equations by Ram P.Kanwal, Academic Press, New York, 2. 1971. For Units III & IV.
- Differential Equations and Calculus of Variations by L.Elsgolts, Mir 3. Publishers, 1970. For Unit V.

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

Programme	: M.Sc. Mathematics.	
<b>Course Title</b>	Core 15: DIFFERENTIAL GEOMETRY	Subject Code : 13PMA4C15
Year	: Second Year	Semester : IV
Hours/Week	: 5	Credits : 4

#### Unit I:

**Curves:** Analytic representation, Arc Length, Tangent, Osculating plane, Curvature Torsion, Formulas of Frenet. **Chapter I: Sections 1.1 - 1.6** 

#### Unit II:

Contact, Natural equations, Helices, General solutions of the Natural equations, Evolutes and Involutes.

Chapter I: Sections 1.7 -1.11

#### Unit III:

**Elementary Theory of surfaces:** Analytic Representation, First Fundamental form, Normal tangent plane, Developable surfaces. **Chapter II: Sections 2.1 - 2.4** 

#### Unit IV:

Second fundamental form, Meusnier's theorem, Euler's theorem. Dupin's indicatrix, some surfaces. The fundamental equations; the equations of Gauss – Weingarten. Chapter II: Sections 2.5 - 2.8 and Chapter III: Sections 3.1 - 3.2

#### Unit V:

The theorem of Gauss and the equations of Codazzi, Some applications of the Gauss and Codazzi equations. The fundamental theorem of surface theory – Geodesic curvature, Geodesics.

Chapter III: Sections 3.3, 3.5, 3.6 and Chapter IV: Sections 4.1 to 4.2

#### **Treatment as in:**

Lectures on Classical Differential Geometry by Dirk, J.Struik, Addison Wesley Publishing Company, 1961.

### **Reference Book:**

- 1. **Differential Geometry: First Course by D. Somasunduram**, Narosa Publishing House, 2010.
- 2. **Differential Geometry : An Integrated Approach by Nirmala Prakash**, Tata McGraw-Hill Publishing Company Ltd. Fourth Reprint, 1992.

## SRI RAMAKRISHNA MISSION VIDYALAYA COLLEGE OF ARTS AND SCIENCE (AUTONOMOUS) COIMBATORE – 641 020. For candidates admitted from academic year 2013-2014 onwards Under New CBCS

### **Programme** : M.Sc. Mathematics.

<b>Course Title</b>	: Elective:4 FLUID DYNAMICS
Year	: Second Year
Hours/Week	: 6

Subject Code :13PMA4EL4 Semester : IV Credits : 4

### Unit I:

Introductory notions – Velocity – Stream lines, and Path of the particle - Stream tubes and Filaments – Fluid body – Density - Pressure, Differentiation with respect to time – Equation of continuity - Boundary conditions( Kinematical and Physical) - Rate of change of linear momentum – Equation of motion of an inviscid Fluid. Chapter I: Sections 1.0 – 1.3, Chapter III: Sections 3.10, 3.20, 3.30, 3.31, 3.40,

## 3.41

## Unit II:

Euler's Momentum theorem - Conservative forces – Steady motion (Bernoulli's equation) – The Energy equation – Rate of Change of Circulation (Kelvin's theorem) – Vortex motion - Permanence of Verticity (Helmholtz Equation). Chapter IIII: Sections 3.42, 3.43, 3.45, 3.50, 3.51, 3.52, 3.53

### Unit III:

**Two dimensional motions** – Two dimensional functions – complex potential basic singularities – source vertex – doublet circle theorem – flow past a circular cylinder with circulation – conformal transformation – Blasius theorem – Lift force.

Chapter 3: Sections 3.1 – 3.7.5 (omit 3.4, 3.5, 3.5.3 and 3.6)

### Unit IV:

Viscous flows – Navier stokes equations – Vorticity and Circulation in a viscous fluid – steady flow through an arbitrary cylinder under pressure – steady couette flow between cylinders in relative motion – steady flow between parallel planes. Chapter 5: Sections 5.2 – 5.3.3

### Unit V:

Laminar boundary layer in incompressible flow boundary layer concept – Boundary layer equations – Displacement thickness – Momentum thickness – Kinetic energy thickness – Integral equation of boundary layer – Flow parallel to semi infinite flat plate - Blasius equation and it's solution.

Chapter 6: Sections 6.2.1, 6.2.3, 6.2.4, 6.3.1

### Treatment as in:

- 1. **Theoretical Hydrodynamics by L.M. Milne Thomson**, Macmillan Company, 5<sup>th</sup> Edition, 1968. For Units I and II.
- 2. **Modern Fluid Dynamics Vol I by N. Curle and H.J. Davies**, D Van Nostrand Company Ltd; London, 1968. For Units III, IV and V

## For candidates admitted from academic year 2013-2014 onwards Under New CBCS

**Programme** : M.Sc. Mathematics.

<b>Course Title</b>	: ELECTIVE 5:CONTROL THEORY Subje	ct Code : 13PM	MA4EL5
Year	: Second Year	Semester	: IV
Hours/Week	:5	Credits	:4

### Unit I:

**Observability:**Linear systems – Observability Grammian – Constant coefficient systems – Reconstruction kernel – Nonlinear systems. **Chapter 2: Sections 2.1- 2.2** 

### Unit II:

**Controllability**: Linear systems – Controllability Grammian – Adjoint systems – Constant coefficient systems – Steering function – Nonlinear systems. **Chapter 3: Sections 3.1- 3.2** 

#### Unit III:

**Stability:**Stability – Uniform Stability – Asymptotic Stability of Linear systems – Linear time varying systems – Perturbed linear systems – Nonlinear systems.

Chapter 4: Sections 4.1-4.3

### Unit IV:

**Stabilizability:**Stabilization via linear feedback control – Bass method – Controllable subspace – Stabilization with restricted feedback. **Chapter 5: Sections 5.1- 5.3** 

### Unit V:

**Optimal Control:**Linear time varying systems with quadratic performance criteria – Matrix Riccati equation – Linear time invariant systems – Non linear systems.

Chapter 6: Sections 6.1-6.3

#### **Treatment as in:**

**Elements of Control Theory by K. Balachandran and J.P.Dauer, Narosa**, 2<sup>nd</sup>Editio, New Delhi.

## SRI RAMAKRISHNA MISSION VIDYALAYA COLLEGE OF ARTS AND SCIENCE (AUTONOMOUS) COIMBATORE - 641 020 For candidates admitted from academic year 2014 - 15 onwards

**Under New CBCS** 

Programme : M.Sc Physics Course Title : Elective : IDE: NUMERICAL ANALYSIS Semester : III Hours/Week : 5 Subject Code: 14PPH3EL3 Year : II Credits : 4

## Unit - I:

The solution of numerical algebraic and transcendental equation: Introduction -Bisection method - Method of successive Approximation or the iteration method - Method of false position (Regula Falsi method) - Newton's Iteration method or Newton-Raphson method.

Simultaneous Linear Algebraic equations: Introduction - Gauss elimination method -Computation of the inverse of a matrix using Gauss's elimination method - Method of triangularisation (or method of factorization) - Crout's method - Iterative methods -Comparison of Gauss Elimination and Gauss Seidal Iteration methods - Relaxation methods examples.

### Unit II:

**Finite Differences**: First differences - Higher differences - Backward differences Central difference notation - Properties of the operator  $\Delta$  - Differences of a polynomial -Factorial polynomials - Relation between the operators E and  $\Delta$  - Relation between the operators (D) and  $\Delta$  - other difference operators - Relationship between the operators -Examples. Interpolation: Central difference tables - Central difference - Interpolation formulae - Gauss's Forward Interpolation formula and Backward Interpolation formulae-

# Examples. **Unit III:**

Numerical Differentiation and Integration: Newton's Forward and Backward Difference Formula to compute the Derivatives - Derivatives using Striling's formula-Trapezoidal rule - Truncation error in the Trapezoidal Formula - Romberg's method - Simpson's rule - Practical Applications of the Simpson's rule - Examples.

### Unit IV:

Numerical Solution of Ordinary Differential Equations: Solutions by Taylor's series -Euler's method - Improved Euler's method - Modified Euler's method - RungeKutta method - Second order RungeKutta method - Higher order RungeKutta method - Examples.

### Unit V:

Numerical Solution of Partial Differential Equations: Solution of boundary value and Initial value problems of partial differential equations - Solution of elliptic, parabolic and hyperbolic partial differential equations.

**Text book:** Numerical Methods in Science and Engineering by Dr M.K. Venkataraman, The National Publishing Company, 5th Edition, 1999.

UNIT 1 Chapter III Sections 1-6 and Chapter IV Sections 1-8

2 Chapter V Sections 1-18.and Chapter VII Sections 1-4.

3 Chapter IX Sections 1-4 & 8-12.

4 Chapter XI Sections 6- 8 & 10- 18.

5 Chapter XII Sections 1-9.